Using atmospheric O2 and CO2 measurements to determine the stoichiometry of photosynthesis and respiration in a temperate forest

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Using atmospheric O\textsubscript{2} and CO\textsubscript{2} measurements
to determine the stoichiometry of photosynthesis and respiration
in a temperate forest

An Honors Paper for the Department of Physics and Astronomy

By Margaret Marie Conley
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Chapter 1

Introduction

1.1 Summary

As humans continue to emit CO$_2$ into the atmosphere via the combustion of fossil fuels, an understanding of carbon sources and sinks is critical to projections of future atmospheric CO$_2$ levels and climate change. CO$_2$ emitted into the atmosphere has three potential destinations. It may be sequestered in the terrestrial biosphere via photosynthesis, it may dissolve in the ocean, or it may remain in the atmosphere, contributing to rising levels of atmospheric CO$_2$ [Keeling et al., 1996]. By enhancing the natural greenhouse effect, rising CO$_2$ levels cause an increase in average surface temperatures, but the degree of warming depends on the abundance of atmospheric CO$_2$. Understanding how much of the CO$_2$ that humans emit will remain in the atmosphere and how much will be stored in biomass on land is therefore necessary to project future warming, ocean acidification, and other changes in the earth system.

Calculation of the land carbon sink requires an accurate value for the O$_2$ : CO$_2$ exchange ratio of photosynthesis and respiration, known as $\alpha_b$ [Battle et al., 2000]. This stoichiometric ratio is the number of O$_2$ molecules produced (or consumed) per CO$_2$ molecule consumed (or produced). Because the ratio depends upon the type of organic matter be-
ing synthesized or oxidized, from simple glucose to more complex molecules, the average value of $\alpha_b$ for the terrestrial biosphere is not well constrained, with a range of potential values from 1.0 to 1.2 [Keeling and Manning, 2014]. Measurements of atmospheric O$_2$ and CO$_2$ in forested regions can help constrain the average value of the O$_2$:CO$_2$ exchange ratio for the forest biome as a whole, since changes in O$_2$ and CO$_2$ in the air over time will be driven by either photosynthesis or respiration and will reflect a range of processes carried out by both plants and soil bacteria over the course of daily and seasonal cycles. However, because the atmosphere is constantly in motion, the ratio of O$_2$:CO$_2$ in the air may also reflect the characteristics of the region from which the air moving through the forest originated, so time periods of analysis must be chosen to maximize local impact and minimize the effect of outside influence.

In this project, we investigate the stoichiometry of O$_2$ and CO$_2$ at Harvard Forest in Petersham, Massachusetts over a span of six years, considering the covariation of O$_2$ and CO$_2$ during 6-hour periods to determine an average value for the stoichiometric ratio of the activity of the terrestrial biosphere. This approach differs from traditional methods of measuring the O$_2$:CO$_2$ exchange ratio using closed chambers or elemental analysis and provides a way to determine the value of this parameter averaged across seasonal cycles and species assemblages. Comparing measurements within and above the canopy and during nighttime and daytime periods, we examine the importance of changing atmospheric dynamics and canopy effects on the observed exchange ratio, and we look for potential seasonal cycles. After our analysis of the observed O$_2$:CO$_2$ exchange ratio, we turn to the question of whether this value is truly representative of $\alpha_b$. We use a simple model to determine the range of variability in CO$_2$ and O$_2$ mixing ratios expected from local influence alone and use this as a criteria to isolate periods dominated by local exchange. This analysis yields important insight into the average value and variability of $\alpha_b$ for temperate forests for use in calculation of the land carbon sink.

The remainder of this chapter provides background information on land carbon
sink calculations, measurement techniques for $\alpha_b$, and atmospheric and seasonal dynamics. Chapter 2 details the process of data collection and calibration. Chapter 3 describes methods used to split the data into 6-hour periods for analysis, the sensitivity of the analysis to time period lengths and fitting processes, and the results for the average stoichiometric ratio. Chapter 4 details the use of spectral analysis to look for seasonal or other cycles in $\alpha_b$, as well as a discussion of seasonal variability in biospheric and fossil fuel signals. In Chapter 5, we use a Lagrangian transport model to investigate changes in the source region of air arriving at Harvard Forest, and we develop a simple 1-D box model to discern the amount of CO$_2$ and O$_2$ variability attributable to local exchange alone. This analysis enables us to understand the relevance of the observed O$_2$ : CO$_2$ exchange ratio as a measure of $\alpha_b$ for the surrounding forest. Chapter 6 describes the results of filtering using friction velocity and CO$_2$ ranges to isolate periods of local influence, which yield a more accurate value of $\alpha_b$ than the entire dataset.

1.2 Background

1.2.1 Carbon sink calculations

Carbon sink calculations partition CO$_2$ uptake into land and ocean fluxes based on key differences between these processes. Terrestrial processes, including fossil fuel combustion, respiration, and photosynthesis, involve the coupled exchange of O$_2$ and CO$_2$. Oceanic uptake and release of O$_2$, however, is essentially decoupled from CO$_2$ fluxes, which are driven by the dissolution and chemical buffering of CO$_2$ in seawater [Keeling and Manning, 2014]. Measurements of atmospheric O$_2$ mixing ratios therefore help distinguish between the uptake of CO$_2$ by the terrestrial biosphere and the ocean. The land and ocean sinks can then be calculated using the known flux of CO$_2$ from cement production and fossil fuel combustion and the mass balance for atmospheric CO$_2$ and O$_2$ (measured relative to N$_2$) along with the stoichiometric ratios of biospheric processes.
and fossil fuel combustion [Battle et al., 2000]:

\[
\begin{align*}
    f_{\text{land}} &= -\frac{\alpha_{\text{ff}}}{\alpha_{b}} f_{\text{fuel}} + \frac{1}{2.49} \frac{d(O_2/N_2)}{dt} \\
    f_{\text{ocean}} &= -\frac{d}{dt} \left( \frac{CO_2}{0.471} + \frac{O_2/N_2}{2.49} \right) - \frac{\alpha_{b} - \alpha_{\text{ff}}}{\alpha_{b}} f_{\text{fuel}} - f_{\text{cement}}
\end{align*}
\] (1.1) (1.2)

where \( f \) terms refer to CO\(_2\) fluxes (negative for ocean and land denoting uptake, positive for cement and fossil fuels denoting emission), \( \alpha_{\text{ff}} \) is the stoichiometric ratio of fossil fuel combustion, approximately 1.4, \( \alpha_{b} \) is the O\(_2\):CO\(_2\) exchange ratio for processes in the terrestrial biosphere, approximately 1.1, and the other coefficients are conversion terms. Because the abundance of O\(_2\) in the atmosphere is much higher than that of CO\(_2\), the fractional variations over time are much smaller, making geochemically informative measurements challenging [Stephens et al., 2007]. In the past 20 years, developments in instrumentation have enabled precise measurement of O\(_2\) over time in field conditions, allowing for an improved quantification of the land and ocean carbon sinks.

### 1.2.2 Measuring \( \alpha_{b} \)

Calculation of the land carbon sink depends on both \( \alpha_{b} \) and \( \alpha_{\text{ff}} \) [Battle et al., 2000]. The stoichiometric ratio for fossil fuel combustion is relatively well-defined, with a global average value of 1.4 [Keeling, 1988]. Although the ratio varies over time and space depending on the mix of fuels being burned, the change from year to year is minimal; from 1996 to 2008, the ratio ranged between 1.39 and 1.42 [Steinbach et al., 2011]. The stoichiometry of photosynthesis and respiration for the terrestrial biosphere, however, is less certain. This ratio depends on the type of reaction taking place in plant cells, which ranges from synthesis of simple glucose during photosynthesis to production of more complex molecules such as lignin or nitrogen-containing molecules [Seibt et al., 2004]. These processes have a range of stoichiometric ratios from 1.0 to 1.2 [Keeling and Manning, 2014]. The value of \( \alpha_{b} \) varies between ecosystems and plant species as well
[Gallagher et al., 2017], and contributions from soil respiration, which vary over time and between soil types [Seibt et al., 2004; Worrall et al., 2013], add to this variability. Further constraining the global average value of $\alpha_b$ will strengthen the confidence of our estimates for the land carbon sink.

Atmospheric measurements of $O_2$ and $CO_2$ may provide a useful method to determine $\alpha_b$, because mixing ratios in the air of a forest will be driven by either photosynthesis or respiration and will reflect a range of processes carried out by both autotrophs and heterotrophs (both plants and soil bacteria) over the course of daily and seasonal cycles. Forest air mixing ratios therefore give an average value of $\alpha_b$ for the forest biome as a whole. Previous studies to determine $\alpha_b$ have used enclosed chambers to measure gas mixing ratios over time as well as analysis of the elemental composition of different types of organic matter. Original studies of soil carbon yielded a ratio of $1.1 \pm 0.05$ [Severinghaus, 1995]. A more recent analysis using the elemental composition of a global survey of soils and vegetation produced a slightly lower value of $1.04 \pm 0.03$ [Worrall et al., 2013]. Measuring this ratio in the atmosphere itself may provide a better value of $\alpha_b$ for calculation of the land carbon sink by integrating the effects of seasonal changes and a heterogeneous landscape. An atmospheric measurement will also help validate the value currently in use for carbon sink calculations.

1.2.3 Atmospheric and seasonal dynamics

Atmospheric mixing ratios of $O_2$ and $CO_2$ depend on a combination of processes. The background abundances (the regional average mixing ratios of these gases in the atmosphere) are altered by exchange with the underlying landscape, including respiration, photosynthesis, and anthropogenic combustion of fossil fuels. Since these processes add and remove $O_2$ and $CO_2$ from the atmosphere according to their respective stoichiometric ratios, changes in the mixing ratios of these gases over time should reflect the stoichiometry of the dominant process driving $O_2$ and $CO_2$ variability. For a predominantly forested
area, this $O_2 : CO_2$ exchange ratio should therefore provide a measurement of $\alpha_b$ for the surrounding ecosystem.

Unfortunately, the ratio of $O_2 : CO_2$ in air does not exclusively reflect the local environment. The atmosphere is constantly in motion, even within the canopy of a forest, and the characteristics of a given parcel of air reflect its evolution as it crosses the landscape, exchanging with forests and cities along its path. This complicates the interpretation of the stoichiometric ratio of $O_2 : CO_2$ measured at a fixed point, because the region from which the air originated (the source region) may change over time. Variation in the mixing ratio of air due to changes in the source region (the background variability) is superimposed on variation due to local exchange, with the latter or both combined driving the changes in mixing ratio observed at a particular location. However, if for a certain time period the observed magnitude of $CO_2$ and $O_2$ variability does not exceed the range of variability potentially driven by local exchange alone, the ratio of $O_2 : CO_2$ will be an accurate measurement of $\alpha_b$.

Both natural and anthropogenic processes that impact $CO_2$ and $O_2$ vary over time, leading to potential temporal variability in $\alpha_b$. Photosynthesis and respiration vary daily and seasonally with forest growth cycles and the activity of soil bacteria. Fossil fuel combustion exhibits its own daily and seasonal cycles associated with rush hours, winter heating, and other energy usage patterns [Steinbach et al., 2011]. Depending on the season and the amount of green space, urban fluxes of $CO_2$ can be similar to or exceed forest fluxes and can therefore have a wide influence on surrounding regions [Velasco and Roth, 2010]. At Harvard Forest, the site studied in this project, the fossil fuel $CO_2$ signal is much smaller than local and regional forest signals during the summer, but the balance changes towards more fossil fuel influence during the winter [Potosnak et al., 1999].

The dynamics of atmospheric exchange vary over time as well. Friction velocity, or $u^*$, is a measure of turbulence that describes the vertical flux of horizontal momentum [Stull, 2006]. During winter, when the canopy is leafless, friction velocities tend to be
higher, and this may influence the relative importance of local exchange and background variability. Surface exchange is limited to the atmospheric boundary layer, also known as the planetary boundary layer (PBL), the section of the atmosphere closest to the ground that interacts with the surface. At night, when the surface cools rapidly, a nocturnal inversion develops, creating a stagnant layer near the surface in which exchange is limited [Stull, 2006]. The forest canopy further impacts air exchange, creating a surface mixing layer in the area underneath the canopy [Raupach et al., 1996]. These changes may lead to variability in the stoichiometry of CO$_2$ and O$_2$, so an investigation of changes in $\alpha_b$ over the course of a year will shed light on both the average value and the amount of deviation from that value due to seasonal changes.
Chapter 2

Data collection and methods

2.1 Experimental setup

The experimental setup is located in Harvard Forest, a 3700 acre Long Term Ecological Research site in the town of Petersham in north-central Massachusetts (42.5°N, 72°W). The site has rolling topography and a temperate climate, with a mixed hardwood and conifer forest dominated by red oak, red maple, black birch, white pine, and Eastern hemlock [Harvard University, 2011]. Harvard Forest has extensive research facilities, including five research towers. Our setup is mounted on the Environmental Measurement Station (EMS) eddy flux tower, a 30 m tower in the Prospect Hill Tract, north of Petersham and east of route 32 at 42.5377°N, 72.1714°W (Figure 2.1).

We measured atmospheric O$_2$ and CO$_2$ concentrations at the Harvard Forest EMS tower from September 2006 to January 2013. Sampling was interrupted in mid-2010 by hardware failures and resumed in May 2012. We sample air from two heights, with one intake at 7.5 m (within the canopy) and another at 29 m (about 5 m above the canopy). Air enters the system through downward-facing aspirated inlets, which helps reduce thermal fractionation [Blaine et al., 2006] (Figure 2.2). The air is transported via tubing down the tower and into a nearby building which houses the analysis instruments (Figure 2.3).
Figure 2.1: Map showing the location of the Harvard Forest EMS tower and Bowdoin College.

Figure 2.2: Photograph of the aspirated inlet at the high intake, designed to reduce thermal fractionation. Image credit: Mark Battle.
Figure 2.3: Diagram of the O$_2$ and CO$_2$ measurement system at Harvard Forest. Shows the path of air arriving from the tower as it passes through filters, chiller traps, and the two analyzers. Also shows the calibration tanks and the valve system used to switch between air sources. Credit: Mark Battle.
Following a design pioneered by Stephens et al. [2007], air flow is controlled using pumps and mass flow controllers. Once the air arrives in the building, it is cooled to remove water using a series of three coaxial stainless steel traps, with the first trap at 5°C and the next two traps at -90°C. As the air exits each trap, 7 µm filters remove particulates and ice crystals. The air is then routed to the O₂ and CO₂ analyzers. Only one airstream can be measured at a time, so the system alternates between the two heights, sending the airstream from the other height to the waste stream. This alternation occurs every 720 seconds, using a cross-over ball valve to switch the flow.

Measurements of O₂ are made with a Sable Systems Oxzilla II fuel cell analyzer, and CO₂ measurements with a LiCor LI-7000 NDIR analyzer. Each analyzer takes in two air streams, a sample and a reference. The mixing ratios in the sample air stream are measured relative to a reference “working” tank of dried air, which also passes through a chiller before entering the analyzer. Measurements are recorded every second. Because the concentration of the working tank may vary over time, the sample air is periodically diverted and replaced by air from one of four calibration tanks that have a known composition. These tanks allow us to correct the differential measurements of the sample stream for drift in either the instrument or the working tank composition. The air stream to be analyzed (standard tank or ambient air) is chosen using two 6-port selector valves. Sampling of ambient air is therefore interrupted for 18-minute calibration runs that occur about four times each day.

Before entering the LiCor CO₂ analyzer, the air stream passes through a mass flow controller and a differential manometer with an automatic metering valve. This ensures that the pressure within the cells of the LiCor remains balanced, because this can change the response of the analyzer. After passing through the LiCor, the air is directed through a 0.5 µm filter and a metering valve before entering the Oxzilla O₂ analyzer. The Oxzilla analyzer can also be affected by pressure differences as well as flow differences between the two cells, so there are metering valves both upstream and downstream of the sensor.
Because the cells may have different biases, we alternate the fuel cell into which each air stream flows using a changeover valve. The difference-of-differences is then calculated:

\[
dd = \frac{((Sa + \delta_1) - (Wt + \delta_2)) - ((Wt + \delta_1) - (Sa + \delta_2))}{2} = Sa - Wt
\]

where \( Sa \) is the sample mixing ratio, \( Wt \) is the working tank mixing ratio, and \( \delta_1 \) and \( \delta_2 \) represent the measurement errors associated with each fuel cell. This calculation accounts for differences in the response of the two cells. We use a procedure described by Keeling et al. [2004] to optimally set the frequency of changeovers. For our equipment, a switching period of 24 seconds maximizes measurement precision while minimizing the loss of measurements due to “dead time” (the time required for the instrument to stabilize after the pressure and flow disruptions associated with changeovers). The data collection set-up is remotely operated by a LabView® program, and data are transferred to a MySQL® database on a server at Bowdoin College.

### 2.2 Data calibration and processing

The raw data are processed to account for switches between air streams, to correct for instrumental drift, and to remove periods with data quality issues. Data collection alternates between atmospheric data and calibration runs, with the atmospheric analysis switching every 12 minutes between high and low intakes. Switching between atmospheric sampling and calibration tanks causes disruptions in pressure and flow. Thus, data collected in the first 432 seconds after a calibration run are discarded to allow the instrument to return to equilibrium. The same 432-second cut is applied following switches between the high and low intakes resulting in a data set of 288-second periods spaced 12 minutes apart, with periodic gaps from calibration runs.

\( \text{O}_2 \) data undergo a further processing step because of the changeovers between
the two cells. The 288 seconds of data from each sampling period are divided into twelve 24-second blocks corresponding to the changeovers between cells. The data for the last 10 seconds of each 24-second block (after the 14-second dead time) are averaged together, and the difference-of-differences is calculated for consecutive pairs of single-block averages, yielding 6 values for each 12-minute sampling period on the chosen intake. These 6 values are averaged to give a single O$_2$ value for that sampling period, with a time stamp corresponding to the middle of the time interval used in calculating the average.

CO$_2$ data are also processed by intake sampling period, but the process is simplified by the absence of changeovers. The 288 seconds of data are divided into the same twelve 24-second blocks as for the O$_2$ measurements. For consistency with the O$_2$ data, the same 10-second periods are used, but rather than calculating a difference-of-differences, consecutive groups of 10 data points are simply averaged together as a group of 20 points, yielding 6 values. These 6 values are again averaged together to yield a single data point with the same time stamp as the O$_2$ data point.

The calibration data from the standard tanks are processed differently from the atmospheric data. After 6 minutes of venting to flush stale gas from the lines, 6 minutes of measurements are recorded. Once the CO$_2$ value measured by the instrument has reached 70% of the change from atmospheric mixing ratios to standard mixing ratios, the remaining data are fitted with the function

$$[CO_2] = A + Be^{-C(t-D)}$$  \hspace{1cm} (2.2)

This gives a value of CO$_2$ in the working tank relative to the standard tank. The O$_2$ measurements are processed using the same difference-of-differences treatment as the atmospheric analysis. After the CO$_2$ record shows that the atmospheric air has been displaced, the last three to five difference-of-differences values occurring after the transition are averaged.
Calibration runs generally occur every six hours and are used to track changes in the working tank and the instrumental response over time. The standard tanks have a wide range of O\textsubscript{2} and CO\textsubscript{2} values, allowing us to check the linearity of the LiCor and Oxzilla analyzers. One of the tanks is run only weekly to check for drifting of the other standard tanks. For the purpose of this research, the amount of drift in the standard tanks is small enough to have no detrimental effect on the results.

Poor quality data collected during periods of malfunctioning equipment or periods that lack calibration data are removed. Finally, the remaining data are adjusted using the calibration runs to correct for drift in the working tank and the instruments.

The calibration runs are also used to determine the instrumental error. For CO\textsubscript{2}, the error is calculated from the scatter of data points about the fitted curve (Figure 2.4), whereas for O\textsubscript{2}, the error is determined using the scatter in the three to five average difference-of-difference values recorded after the instrument reaches equilibrium with the standard tank. These errors varied over time (Figure 2.5). When fitting lines to plots of O\textsubscript{2} vs. CO\textsubscript{2}, we split the data set into three time periods and used representative CO\textsubscript{2} and O\textsubscript{2} error values for each (Table 2.1).

Our final set of CO\textsubscript{2} and O\textsubscript{2} measurements was then augmented with friction velocity values measured at the Harvard Forest EMS tower [Munger, 2018]. The u* values were matched to individual CO\textsubscript{2} and O\textsubscript{2} values (where each value represents the result of the averaging process for each 12-minute sampling period). Friction velocity has the potential to influence the observed stoichiometry and is used in Section 6.2 to create subsets of data that reflect particular environmental parameters.
Figure 2.4: Plot of CO\textsubscript{2} vs. time for a calibration run, showing the curve (in green) fitted to the data points (in blue) about which the scatter is calculated to determine the instrumental error in CO\textsubscript{2} measurements.

<table>
<thead>
<tr>
<th>Time period</th>
<th>Uncertainty in CO\textsubscript{2} (ppm)</th>
<th>Uncertainty in O\textsubscript{2} (µmol/mol)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Sept. 2006-July 2009</td>
<td>0.02</td>
<td>1.5</td>
</tr>
<tr>
<td>July 2009-July 2010</td>
<td>0.05</td>
<td>7.3</td>
</tr>
<tr>
<td>May 2012-Jan. 2013</td>
<td>0.13</td>
<td>11.7</td>
</tr>
</tbody>
</table>

Table 2.1: Uncertainty in CO\textsubscript{2} and O\textsubscript{2} measurements. Uncertainty differed between time periods because of variability in the stability of the instruments. The increase in uncertainty near the end of the study period may be due to problems with system gas tightness.
Figure 2.5: Error in CO₂ (top, in green) and O₂ (bottom, in blue) plotted against serial number, which corresponds to the chronological order of data points. Error varied over time and tended to increase significantly at the end of the study period. We speculate that this increase in error may be due to problems with system gas tightness.
Chapter 3

Analysis of the average stoichiometric ratio

3.1 Data categorization and analysis

We calculate $\alpha_b$ by analyzing the covariation of $O_2$ and $CO_2$ over time. For a plot of $O_2$ vs. $CO_2$, the slope of a linear fit gives the stoichiometric ratio of $O_2$ to $CO_2$, which for an atmospheric composition dominated by the terrestrial biosphere gives $\alpha_b$. We aggregate the data into one-day periods and split them by intake height and time of day before calculating the slopes, which allows us to examine the effects of atmospheric and boundary layer processes on the observed stoichiometry. Each one-day period includes a daytime interval from 9am–3pm and a nighttime interval from 10pm–4am. The split between high and low intakes results in four subsets of data for each one-day period: day/high, day/low, night/high, and night/low. Examples of these plots are shown in Figure 3.1.

The duration of the aggregation period determines the effective “footprint” of the tower over that time period, where “footprint” refers to the area that contributes to the observed atmospheric composition at Harvard Forest. The size, composition, and
Figure 3.1: Example of scatterplots of $O_2$ vs. $CO_2$ for the four subsets of data: day and night at high and low intakes. These plots are for 9am–3pm on 21 July and 10pm–4am on 21–22 July in 2007. The color of the points indicates the time at which each data point was taken (in local time). Note the overall decrease in $CO_2$ and increase in $O_2$ during the daytime interval, driven by photosynthesis, and the overall increase in $CO_2$ and decrease in $O_2$ during the nighttime interval, driven by respiration. The red line shows the results of a Deming regression (described in Section 3.1), and the slope, corresponding to the $O_2 : CO_2$ exchange ratio, is indicated above each plot.
variability of this footprint are all important in determining the relevance of the observed \( \Omega_2 : \Omega_{CO_2} \) ratio as a measurement of \( \alpha_b \). As parcels of air move across the landscape, passing over forests, cities, suburbs, and roads, they exchange \( \Omega_2 \) and \( \Omega_{CO_2} \) with the surface. One-day periods (additionally separated into daytime and nighttime intervals) yield more informative slopes than longer spans of multiple days because the source region of incoming air is smaller for a shorter time period \( [Gerbig et al., 2006] \). The source region is also less variable over time and likely includes a landscape dominated by forest with a small influence from fossil fuels (see Section 5.2).

The daytime and nighttime intervals also affect the region of influence reflected in the observed slope value. We calculated the slope values for both 6-hour intervals (as described above) and 4-hour intervals (10am–2pm for day, 11pm–3am for night) to explore the impact of interval length on our results. Our definition of daytime and nighttime intervals is based on \( u^* \), the friction velocity. Nighttime is characterized by lower \( u^* \) values due to higher stratification and limited vertical exchange, as air near the surface is trapped by a nocturnal stable boundary layer \( [e.g. Stull, 2006] \). This may lead to a more local signal in the observed stoichiometry. In contrast, daytime is characterized by higher \( u^* \) values indicating more exchange and vertical air movement, and consequently a potentially larger footprint influencing observed mixing ratios.

We used 24 years of \( u^* \) data from the EMS tower at Harvard Forest to calculate an hourly climatology of average \( u^* \) values for each hour of the day (Figure 3.2). The daily variation in \( u^* \) shows a somewhat sinusoidal cycle, with higher \( u^* \) values during the day, peaking around noon, and lower \( u^* \) values throughout the night. We used this climatology to choose daytime and nighttime intervals that are dominated by the maximum and minimum \( u^* \) values, respectively, avoiding transition periods because of the variability in sunrise and sunset times throughout the year. Although \( u^* \) also shows pronounced seasonal cycles, with higher values in winter (Figure 3.3), as well as short-term variability due to high winds and storms, the daytime and nighttime splits are applied year-round
as a first-order approximation for stratified and well-mixed regimes. These regimes may in turn exhibit more or less local influence on the observed stoichiometry.

Figure 3.2: Hourly values of friction velocity (u*, cm/s). Green dots show hourly u* values for 1991-2015 measured at the Harvard Forest EMS tower, and the blue points and line show the hourly average. Although u* is highly variable, with a large amount of scatter for each hour of the day, standard errors on the hourly averages are too small to be seen on the plot, and the climatology is well constrained. Data courtesy of Harvard Forest online archives [Munger, 2018].

High and low intake heights may also exhibit different stoichiometry due to the “surface layer” created by the forest canopy. This surface layer, which exists within the larger planetary boundary layer (PBL), is characterized by a pronounced inflection point
Figure 3.3: Seasonal variability in $u^*$ (cm/s). Green dots show the average $u^*$ value for each day of the year, calculated from hourly data for 1991-2015. The blue line shows the results of a loess smoothing function using a window of 36.5 days. Friction velocity tends to be higher and more variable in the winter months compared to the summer.
in velocity at the top of the canopy, accompanied by maximum shear and an increase in wind speed [Raupach et al., 1996]. The high intake on the EMS tower, therefore, is in a transition zone between low velocities within the canopy and higher velocities above. Within the canopy, turbulence and coherent eddies transport and mix air parcels, contributing to vertical exchange [Raupach et al., 1996]. At night, stable stratification can weaken mixing and lead to the accumulation of CO$_2$ and other gases within the canopy, especially at low points in the landscape [de Araújo et al., 2008]. Stratification may increase the relative influence of local signals at the low intake compared to the high intake. However, canopy waves can develop under stably stratified conditions, leading to vertical mixing, and rolling topography can further complicate the flow of wind within the canopy [Lee, 2000]. These dynamics may contribute to potential differences in stoichiometry between high and low intakes.

We use the slopes of linear fits to scatter plots of O$_2$ vs. CO$_2$ to calculate the O$_2$ : CO$_2$ exchange ratio. Slopes are calculated using a Deming regression, a type of orthogonal fit that takes into account significantly different errors in the x and y variables [Deming, 2011]. Before performing the regression, daytime or nighttime intervals with too few data points (fewer than three) are removed. Then an iterative process is used to remove outliers before calculating the final fit. After calculating an orthogonal fit to the data set along with the orthogonal residuals and the standard deviation of the residuals ($\sigma_{res}$), points with a residual greater than $4\sigma_{res}$ are cut from the data set, and the process is repeated until the data set converges and no points have a residual greater than $4\sigma_{res}$ (Figure 3.4). The slopes are negative because increases in CO$_2$ coincide with decreases in O$_2$, and vice versa.
Figure 3.4: Scatterplots of O₂ vs. CO₂ for 14–15 June 2012 at the low intake. The empty circle denotes a point that was removed by the orthogonal residual cut and was not included in the final fit shown by the red line.

### 3.2 Averaging of slopes and sensitivity tests

Using the slopes for each of the 3760 6-hour periods, we calculate an average value for the O₂ : CO₂ exchange ratio separately for the low and high intakes during daytime and nighttime intervals, as well as an overall average including both intakes and intervals. To determine a representative average slope value, we examined the distribution of slopes. Based on histograms and normal probability plots that show the degree to which the distributions of slopes fit a normal distribution, the distributions for both the aggregation of all slopes and the four subsets have Gaussian cores but non-Gaussian tails (Figures 3.5 and 3.6). We expect the aggregation of all slopes in particular to be non-Gaussian, because it consists of four potentially different distributions of slopes for day/high, day/low, night/high, and night/low subsets.

Given the non-Gaussian tails, we employ an iterative averaging of the slope values. We average all slopes and calculate the standard deviation, then discard slopes more than nσ away from the mean. We then recalculate the average and iterate until convergence, when no points remain outside the nσ window. We considered both n = 3 and n = 4 to test the sensitivity of our results to this procedure. Results are summarized in Table 3.1.
Figure 3.5: Distribution of slopes for the entire dataset after the iterative cut. The top left panel shows the iteratively cut slopes plotted against time in decimal years; gaps indicate periods where no data were collected. The top right panel shows a histogram of the iteratively cut slopes. The bottom left panel shows a normal probability plot for the entire dataset after the first iteration of the iterative cut, whereas the bottom right shows the same plot after the iterative cut was completed, demonstrating the reduction of the dataset’s non-Gaussian tails. The dotted lines in the normal probability plots indicate the point pattern expected for a normal distribution. Summary statistics are in Table 3.1.
Figure 3.6: Histograms and normal probability plots for the four data subsets. Each normal probability plot corresponds to the histogram to its left. Although the iterative cut partially normalizes the distributions, there are still non-Gaussian tails, visible in the normal probability plots, in which the dotted line indicates the point pattern expected for a normal distribution. For this reason, we include both the means and the medians for comparison in the summary statistics in Table 3.1.
Figure 3.7: Plot of slopes vs. time in decimal date. Point colors indicate the time interval and intake height for each data point. The increase in spread towards the end of the study period may be a reflection of the increase in measurement error shown in Figure 2.5.
After a $3\sigma$ cut, the difference between the mean and median values is smaller, indicating that the cut reduces the non-Gaussian tails of the data set, although the mean and median do differ, especially for some subsets of the data such as day/low. For a $4\sigma$ cut, the difference between mean and median values is larger, and although the median values are similar to those produced by the $3\sigma$ cut, the mean values are quite different. This justifies the use of a relatively narrow $3\sigma$ window to remove outliers and normalize the distribution of slopes.

Although we considered other techniques to remove outlier slope values, none proved able to systematically remove poor fits. The error in the slope calculated during the regression process was highly variable, with some clearly flawed fits achieving low uncertainty due to an anomalously large range in $O_2$ or $CO_2$ (Figure 3.8). In other cases, an isolated point with an anomalously large $O_2$ or $CO_2$ value had a disproportionate impact on the slope (Figure 3.9). The cause of these high $O_2$ and $CO_2$ values is unknown. Values of chi-squared for the slopes proved similarly variable, with no clear trend of higher values for poor fits. The large number of slope plots (3760 total) meant that we were unable to identify obviously inappropriate fits by visual inspection.

![Figure 3.8: Scatterplot of $O_2$ vs. $CO_2$ for the nighttime interval on 15–16 October 2008.](image)

Although the linear fit is obviously inappropriate for this plot, the uncertainty in the regression is low. This is due to the anomalously large ranges in $CO_2$ and $O_2$, which are much higher than the ranges characteristic of the majority of the plots.
<table>
<thead>
<tr>
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<th>Iterative cut</th>
<th>Data set</th>
<th>mean</th>
<th>median</th>
<th>SD</th>
<th>SEM</th>
<th>N</th>
<th>N cut</th>
<th>N iter</th>
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<td>3σ</td>
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<td></td>
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<td>0.01</td>
<td>3009</td>
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<td>-1.09</td>
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<td>0.01</td>
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<td>164</td>
<td>22</td>
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<td>-1.08</td>
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<td>0.01</td>
<td>723</td>
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<td>19</td>
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<tr>
<td>6-hour</td>
<td>4σ</td>
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<td>0.01</td>
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<td>-1.09</td>
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<td>0.02</td>
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<td>71</td>
<td>12</td>
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<td>0.02</td>
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<td>16</td>
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Table 3.1: Table of average values for all slopes and the four data subsets, including mean, median, standard deviation (SD), standard error of the mean (SEM, defined as SD/√N), number of slopes values (N), number of slope values cut during the iterative process (N cut), and the number of iterations before convergence (N iter). Shown are the statistics for two interval lengths, 6 hours and 4 hours, as well as two iterative cutting windows, 3σ and 4σ, to test the sensitivity of the resulting average values to those parameters. Because the 4σ window results in a larger discrepancy between mean and median values, and the 4-hour interval increases uncertainty without significantly changing the average slope values, we concluded that the 6-hour, 3σ combination provides the best results.
Figure 3.9: Scatterplots of O\textsubscript{2} vs. CO\textsubscript{2} for 3–4 October 2007. In the “Day, High Intake” plot, an anomalously high CO\textsubscript{2} value resulted in a non-representative fit without much increasing the uncertainty, while the other subsets, whose linear fits are much more representative of the trend in the data, have higher uncertainties. Similar to Figure 3.8, a point with a much higher CO\textsubscript{2} or O\textsubscript{2} value than the rest of the data causes problems for the linear regression and results in low uncertainties that do not reflect the actual quality of the fit.

We also compared statistics for 6-hour and 4-hour daytime and nighttime intervals, with the nighttime interval centered about 1am and the daytime interval centered about noon. Besides testing the robustness of the average slope value, this comparison helps us determine whether a shorter time period might significantly enhance the local signal in the slope values by further reducing variability in the source region. The 4-hour interval data set has fewer slope values overall, because the shortened interval reduces the number of available data points. This reduction of data points resulted in slightly larger standard deviations for all subsets of the data except night/low. For all subsets, the mean values for the 4- and 6-hour intervals are within one standard deviation of each other, and the median values differ even less. Because there is no notable change in the
average slope values, we concluded that 4-hour intervals simply reduce the number of data points and the statistical power of the analysis without altering the value of the $O_2:CO_2$ exchange ratio. Therefore, we use 6-hour intervals for our calculation of $\alpha_b$. Histograms, normal probability plots, and scatterplots for all slopes and the four subsets are shown in Figures 3.5, 3.6, and 3.7.

### 3.3 Discussion of results for the average stoichiometric ratio

Based on our analysis of the distribution of slope values, we believe that the mean provides the value of the stoichiometric ratio most representative of the underlying ecosystem processes. The iterative cutting process at least partly normalizes the slope distributions, and the medians and means are consistent within less than one standard deviation. In addition, the relative magnitudes of the means for the four data subsets (low vs. high and day vs. night) are consistent both for changes in the daytime and nighttime interval length and changes in the iterative fitting window. Mean and median slope values for all slopes and the four subsets are shown in Table 3.1.

Our all-data slope value of $-1.06 \pm 0.01$ (taking the absolute value of the slope to obtain the exchange ratio) is in agreement with the values for $\alpha_b$ calculated by both Severinghaus [1995] and Worrall et al. [2013], although it is in the low end of the range reported by Severinghaus. This value is also lower than the standard value of 1.1 used in most calculations of the land carbon sink [Keeling and Manning, 2014]. If our measurements reflect mainly local influences and are representative of a predominantly forested landscape, they support the use of a slightly lower value of $\alpha_b$ (1.05–1.07) in such calculations. Even if our data represent a mix of forest fluxes with a small amount of fossil fuel influence, the addition of fossil fuels would raise the value of $\alpha_b$ above its true value, in the direction of $\alpha_ff$ (1.4). This gives further support to an adjustment in the value of
The slope values for the four subsets of data provide a perspective on the influence of atmospheric processes in determining observed slope values. The night/high subset has the steepest slope, with a mean of \(-1.11 \pm 0.01\), followed by day/high \((-1.06 \pm 0.01)\), night/low \((-1.04 \pm 0.01)\), and day/low \((-0.97 \pm 0.01)\). The difference between day and night slopes, with more negative values at night for the same intake height, could result from several factors. Fossil fuel influence may be more apparent at night, when gas fluxes from forests are reduced but fossil fuel combustion decreases only slightly from daytime values (see Figure 5.7). Steeper nighttime slopes may also reflect changes in the dominant plant physiological processes occurring in the forest, such as the production or respiration of more nitrogen-rich molecules with higher stoichiometric ratios [Keeling and Manning, 2014]. Soil respiration may influence the slopes observed at night, especially at the low intake. Although stably stratified conditions at night may enhance local influence, periodic gusts of wind may nullify this effect. Shallower slope values during the day may, in turn, reflect an increased influence of forest fluxes relative to fossil fuel influence, pulling the exchange ratio closer to 1.05, or the dominance of photosynthesis over respiration altering the exchange ratio.

The difference between high and low intakes likely results from the impact of the canopy surface layer. Reduced air velocities within the canopy may enhance local influence and drive slope values towards \(\alpha_b\). At night, stratification may increase the isolation of the high intake from the low intake and result in background variability rather than local influence dominating the signal at the high intake. The day/low slope is particularly shallow compared to the other subsets and the average of all slopes, at the low end of values for the \(O_2 : CO_2\) exchange ratio calculated by Worrall et al. [2013]. In contrast to the atmospheric boundary layer, which becomes stably stratified near the surface at night, the forest canopy can be more stable during the day than at night, because it is warmed from above by incoming sunlight, and this may drive the exchange
ratio towards smaller values for the day/low subset. At night, with cooler air above the treetops, upside-down thermals can mix the air within the canopy [e.g. Stull, 2006; Jacobs et al., 1992], perhaps leading to relatively steeper slope values for the night/low subset.
Chapter 4

Seasonal cycles in atmospheric stoichiometry

4.1 Spectral analysis of slopes

We used spectral analysis to look for the presence of cycles in the slope values. Because our data are not evenly spaced, we used Lomb-Scargle periodograms to quantify the temporal structure of the data [Press et al., 2007]. We created a power spectrum for all 6-hour slopes together, as well as spectra for the four subsets of data separately. Slopes were assigned times based on the approximate midpoint of each 6-hour period. The resulting periodograms include a power spectrum and an estimate of the significance of any peaks.

The four subsets and the combined slopes exhibit several different periodicities (Figures 4.1 and 4.2). Although the power of the peaks is relatively low overall, several peaks are significant at the $\alpha = 0.05$ level. For all slopes combined, there is a broad peak encompassing frequencies from 0.4 to 1.0 cycles per year (Figure 4.3) with one significant spike, indicating a one- to two-year cycle. For the night/low and day/high subsets, a significant peak appears at approximately 18 cycles/year, corresponding to a period of
about three weeks. This peak is significant at the $\alpha = 0.01$ level for the day/high slopes. The night/high subset has a significant peak at 1 cycle/year, while the day/low subset exhibits a peak at 0.6 cycles/year; cycles with frequencies of 18 are not apparent in these two data subsets, nor for all slopes combined.

Figure 4.1: Lomb-Scargle periodogram for the entire set of slopes (after the iterative cut described in Section 3.2), showing the power spectrum for a range of frequencies in cycles/year. Dashed lines indicate the power thresholds for the indicated significance levels. For all slopes combined, there is evidence of a low frequency peak with no significant peaks at higher frequencies.

Several of these periodicities broadly correspond to a yearly seasonal cycle. This cycle is clearly apparent in the night/high subset, and the all slopes and the day/low subset have periodicities close to one cycle/year. A comparison of the average slope value for winter (slopes from the months of December, January, and February) and summer (from the months of June, July, and August) reveals significantly different average values.
Figure 4.2: Lomb-Scargle periodograms for the four subsets of slopes (after the iterative cut), showing power spectra for a range of frequencies in cycles per year. Dashed lines indicate the power thresholds for the indicated significance levels. For day/high and night/low subsets, significant peaks occur at a frequency of approximately 18 cycles/year (a period of three weeks), which we speculate may be due to the timing of calibration runs rather than an actual environmental signal. The day/low and night/high subsets show significant peaks at 0.6 and 1.0 cycles/year, close to a seasonal period of one year.
Figure 4.3: The same plot as in Figure 4.1 magnified to show the power spectrum in the low frequency range. A broad peak is evident from 0.4–1.0 cycles per year, with a significant spike at 0.4. A period of approximately one year may reflect a seasonal cycle in slopes.
(Table 4.1, Figure 4.4). The steeper slopes in winter, closer to $\alpha_{ef}$, likely indicate an increase in fossil fuel influence during that season, when fossil fuel use remains steady or increases in the northeast due to energy use for heating while the biosphere is dormant and plant gas fluxes are small. This is consistent with the winter increase in CO$_2$ from fossil fuels at Harvard Forest observed by Potosnak et al. [1999]. Noise in the data may have obscured a stronger seasonal cycle, leading to the lack of a seasonal cycle in certain subsets of the data and periodicities varying from the expected value of one cycle/year.

<table>
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<th>Season</th>
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<th>SD</th>
<th>SEM</th>
<th>N</th>
</tr>
</thead>
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<td>0.22</td>
<td>0.01</td>
<td>1007</td>
</tr>
<tr>
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<td>-1.15</td>
<td>0.44</td>
<td>0.02</td>
<td>441</td>
</tr>
</tbody>
</table>

Table 4.1: Average values for slopes categorized by season. Winter includes the months of December, January, and February; summer includes June, July, and August. Averages were calculated using the iteratively cut data set described earlier in Section 3.2. Significantly more negative slopes in winter may reflect increased fossil fuel influence. SD, standard deviation; SEM, standard error of the mean; N, number of data points.

Aside from a shifting balance between fossil fuels and the biosphere, a seasonal cycle in slope values could also be driven by cycles in plant physiological processes. Depending on the season, trees may produce different types of molecules with different stoichiometric ratios [Seibt et al., 2004], although Gallagher et al. [2017] found that the oxidative ratio of leaves and tree rings was invariant throughout the year. Intense growth and photosynthesis in the summer contrast with reduced or absent photosynthesis during the winter, when fossil fuel influence also increases. Seasonal cycles in $u^*$ may increase the importance of local exchange during the summer and background variability during the winter, potentially contributing to a yearly cycle as well as the difference in winter vs. summer average slope values.

The three week cycle that appears in the day/high and night/low subsets is perplexing. Although potentially the result of some environmental factor, such as the passage of fronts, this cycle is possibly the result of an experimental factor, such as the
Figure 4.4: Histograms for winter and summer slope values. Winter comprises the months of December, January, and February and summer comprises June, July, and August. Winter slopes have a more negative mean value, closer to the stoichiometric ratio for fossil fuel combustion, although the sample size is smaller for winter than for summer. Statistics are shown in Table 4.1.
periodic runs of calibration tanks. One of the calibration tanks (the low frequency tank) is run approximately every three weeks, potentially producing a three-week cycle in the periodograms. This cycle might be more apparent in certain subsets of data if the low-frequency tank calibration runs were to occur, by chance, more often during day/high and night/low periods. This possibility will be explored in future work.

4.2 Analysis of environmental variables

To investigate potential drivers of the one year seasonal cycle observed in the slope data, we performed spectral analysis on a range of variables measured at the Harvard Forest EMS tower, including air temperature, net ecosystem exchange (NEE), ecosystem respiration, photosynthetically active radiation (PAR), and friction velocity ($u^*$) [Munger, 2018]. All of these variables show strong, highly significant periodicities at seasonal (1 cycle/year) and daily (365 cycles/year) frequencies, with harmonics appearing at multiples of these frequencies. The yearly cycle corresponds with the yearly cycle observed in the slope data. In contrast, these environmental variables do not produce a peak at a period of three weeks, further indication that this cycle in the slope values may be an artifact of the sampling and calibration procedures.
Chapter 5

Modeling air transport and exchange

5.1 Introduction

A central concern in the preceding analysis is the link between our average slope value and the average O$_2$ : CO$_2$ exchange ratio for the terrestrial biosphere, $\alpha_b$. After deriving a representative average for the stoichiometric ratio from our 6-hour plots, we must evaluate whether this slope provides an accurate measurement of $\alpha_b$ or simply reflects variability in the “background” composition. Only a local influence will give a representative value of $\alpha_b$ for a temperate forest; background signals reflect a mix of fossil fuel and biosphere influence from across the country which will vary with changes in the source region of air. The balance of local and background signals that we observe depends on both the size of the signals and on the dynamics of the atmosphere and boundary layer.

Ideally, we would subtract the variability of the background air upwind of Harvard Forest from our observations to extract a local signal. However, measurements of this background air do not exist, nor do we know what slope the background variability would have. Therefore, we use a different metric of background influence: the range of mixing ratios of both CO$_2$ and O$_2$ over 6-hour intervals. Variability driven by changes in the background (i.e. changes in the source region of the air) will be superimposed on local
exchange, so that a range in CO$_2$ and O$_2$ larger than that produced by local exchange alone must be driven by background variability in addition to local influence.

In the following chapter, we first use a Lagrangian model of atmospheric transport to investigate variability in the source region for air arriving at Harvard Forest. We then address the local vs. background question by considering whether a simple model of purely local fluxes can explain the full range of CO$_2$ and O$_2$ variability that we observe in our 6-hour intervals. If so, this increases our confidence in our interpretation of slopes as indicators of $\alpha_b$. We also use the model to understand the relationship between surface fluxes, atmospheric transport, and predicted slopes.

### 5.2 Modeling of atmospheric transport

To examine variability in the source region and the geographic path of air arriving at Harvard Forest over the course of a 6-hour period, we used a Lagrangian model of atmospheric transport. HYSPLIT is an online atmospheric transport and dispersion model available on the National Oceanic and Atmospheric Administration (NOAA) website [NOAA, 2018]. For a specified location and sampling time, the model uses archived, gridded observations of winds, temperature, and pressure to calculate the past trajectory of an air parcel, which represents a set of properties for a given air mass [Stein et al., 2015]. We used the model to create back-trajectories for air parcels arriving at Harvard Forest over a range of dates and times, during winter and summer as well as daytime and nighttime periods.

Using multiple sequential trajectories started every hour, we observed changes in the source region of Harvard Forest air over time. The source region for our study site typically lies to the west, including parts of southern Vermont, western Massachusetts, New York, and Pennsylvania. This occasionally varies to include Boston, Maine, and even the southern coastal region for longer time periods (Figure 5.1). The distance
traveled in a 6-hour period varies from approximately 50 to 200 km for the sample of 6-hour trajectories we created (Figure 5.2). Not surprisingly, longer periods show parcels traveling greater distances (compare to Figure 5.1). Limiting the time period analyzed to six hours therefore appears to restrict the source region to a modest, fairly homogeneous area. This source region may include small urban centers (such as Albany, Springfield, and on occasion, Boston) but for the most part consists of relatively rural, forested regions.

Although the source region does vary over time, even for a single six hour period, changes tend to be small. Seasonal variability in wind speed and the passage of fronts likely cause greater changes in this source region on certain days (Figures 5.3 and 5.4). To understand the relative importance of this source region variability, we need to understand the range of variability in CO$_2$ and O$_2$ potentially driven by local exchange. If the range of variability that we observe can be explained by local influences alone, our 6-hour slope values should reflect a signal dominated by the terrestrial biosphere, with some contamination from fossil fuel signal. While multi-day aggregation of data would provide greater statistical power, Gerbig et al. [2006] show that the region of influence grows rapidly to continental scales with increasing time periods, defeating our efforts to characterize a biospheric signal.

5.3 Investigation of CO$_2$ and O$_2$ variability using a 1-D box model

We created a simple one-dimensional box model to better understand the importance of local influence vs. background variation in our slope plots. We consider parcels of air starting at the beginning of a hypothetical 6-hour trajectory moving over a simple landscape, and we record the CO$_2$ and O$_2$ values that result at the endpoint of this trajectory.
Figure 5.1: 24-hour back-trajectories for Harvard Forest produced by the HYSPLIT model, starting on 18 December 2012. Each trajectory shows the path of an air parcel during the 24 hours before it arrived at Harvard Forest. Trajectories were started at 6-hour intervals, moving back in time, to create the ensemble of trajectories shown. For this longer time period, the source region is highly variable and encompasses a large area, demonstrating our rationale for using a shorter 6-hour interval for our slope plots to reduce source region variability.
Figure 5.2: A set of 48 6-hour back-trajectories produced by the Hysplit model, plotted on satellite imagery from Google Earth. Each trajectory shows the path of an air parcel during the 6-hour period before it arrives at Harvard Forest. Trajectories include 24 daytime and 24 nighttime trajectories for two days in winter and two days in summer. For each day, trajectories were started each hour between 9am–3pm and 10pm–4am, the same time intervals used for the slope plots. These 6-hour intervals encompass a fairly consistent source region with a radius of 50–200 km. The area is mostly forested with some small urban centers.
Figure 5.3: 6-hour back trajectories for Harvard Forest on 24 Jan 2009, with one trajectory started each hour between 9am and 3pm EST (corresponding to the 6-hour daytime interval used to calculate slopes), showing variability in the source region over that time period. This particular day shows a steady shift in the source region over time, although the path length and general source area remain similar. For this period, background variability might have a slightly stronger influence on the observed CO$_2$ and O$_2$ variability at Harvard Forest.
Figure 5.4: 6-hour back trajectories for Harvard Forest on 2 Feb 2015, with one trajectory started each hour between 10pm and 4am EST (corresponding to the 6-hour nighttime interval used to calculate slopes), showing variability in the source region over that time period. For this particular night, changes in the source region were minimal, with air coming from a small area in southwestern NH, so local influence would likely dominate the observed CO$_2$ and O$_2$ variability at Harvard Forest.
over time. By providing a sense of the range of CO$_2$ and O$_2$ variability produced by local exchange, this model helps distinguish between local influence and background variability. Rather than making quantitative predictions of CO$_2$ or O$_2$ for particular days, we seek to quantify the range of variability based on plausible estimates of surface fluxes and boundary layer heights.

The model calculates slope values resulting from a simplified scenario of land-atmosphere exchange over 6-hour periods. Each air parcel enters the first box of the model with a given “source” concentration of O$_2$ and CO$_2$. The model has 30 boxes, each representing the location of the air parcel at 12-minute intervals during the 6 hours it takes to travel from the first box of the model to the last box, when the air parcel arrives at Harvard Forest (Figure 5.5). As each parcel passes through each box, it exchanges O$_2$ and CO$_2$ with the landscape underneath that box. Any O$_2$ or CO$_2$ emitted or taken up by the landscape is added to or removed from the box volume, changing the mixing ratio of O$_2$ and CO$_2$ in the box based on the volume of the box and the magnitude of the flux using the relationship:

$$C_{\text{final}} = C_{\text{initial}} + \frac{F \cdot t \cdot 22.4}{h \cdot 1000}$$

where C is the mixing ratio of O$_2$ or CO$_2$ in ppm, F is the flux from the landscape underneath the box in $\mu$mol/m$^2$/s, t is the length of the time interval over which the flux occurs in seconds, h is the height of the box in m, and the factors of 22.4 (the molar volume) and 1000 convert moles to liters and liters to m$^3$, respectively. We use one half of the PBL height as the box height, based on the value used in more sophisticated models of atmospheric transport [Maryann Sargent, personal communication; Lin et al., 2003]. The O$_2$ and CO$_2$ values for each parcel change due to the fluxes from the landscape type beneath each box. We then shift the parcels forward by one box. After 24 hours of spin-up time to allow several parcels to pass through the entire sequence of boxes, the
O₂ and CO₂ concentrations of parcels are recorded as they arrive in the final “Harvard Forest” box at the end of the 30-box sequence. The time values are also recorded and slopes calculated separately for the same 6-hour daytime and nighttime intervals as the observed data to allow for comparisons in the range of CO₂ and O₂ variability over time.

Figure 5.5: A conceptual diagram of the box model. Only 6 of the 30 boxes are shown, denoting the locations of the air parcel at each hour along its path to Harvard Forest. Air enters the model from the left (the source region) and leaves the model on the right (at Harvard Forest). As the air parcels travel through each box, O₂ and CO₂ are exchanged between the boxes and the landscape, which changes the mixing ratio of the parcel. The parcels shift forward every 12 minutes, and their mixing ratios are recorded as they arrive in the final “Harvard Forest” box on the right.

To parametrize fluxes of CO₂ from a forested landscape, we used CO₂ flux data from the Harvard Forest EMS tower [Munger, 2018]. Forests have negative CO₂ flux around noon, indicating uptake due to photosynthesis, and positive fluxes at night due to respiration. The hourly averages are based on 24 years of eddy flux measurements. Because fluxes vary greatly between winter and summer, we calculated separate climatologies for summer (June, July, and August) and winter (December, January, and February). We assumed an O₂ cycle of opposite sign with 1.05 times the magnitude of the CO₂ cycle, based on the most recent values of α_b from the literature [Worrall et al., 2013] as well as our results. These daily cycles are shown in Figure 5.6.

To parametrize fossil fuel CO₂ fluxes, we used published CO₂ flux records collected in a range of urban and suburban areas. CO₂ fluxes vary depending on the size
Figure 5.6: An hourly climatology of CO$_2$ fluxes at Harvard Forest based on hourly eddy flux data from 1991–2015, separated into winter and summer climatologies. Green dots show the ensemble of hourly data points, and the blue points and line show the average value for each hour. Summer fluxes have much higher magnitudes and a more pronounced daily cycle than winter fluxes, which are low, slightly positive (due to respiration) and fairly constant. One outlier in the summer plot (hour 23, flux 107.7 $\mu$mol CO$_2$/m$^2$/s) was omitted for clarity.
of the city and the area of green space, but tend to be positive at all times. CO₂ flux increases around 6am with the morning rush hour, followed by some drawdown at noon due to urban vegetation and a second peak around 6pm associated with the evening rush hour [Bergeron and Strachan, 2011; Velasco and Roth, 2010; Ward et al., 2015]. Using a simplified model of this CO₂ cycle, we created a corresponding model of urban O₂ fluxes, assuming a stoichiometric ratio of 1.4 for fossil fuel combustion. For simplicity, we neglected the influence of urban vegetation on the stoichiometry. We also created CO₂ and O₂ cycles for a more suburban landscape, again based on eddy flux measurements taken in suburban areas [Bergeron and Strachan, 2011], with lower flux values overall due to reduced population density and increased green space. This may be more representative of the urban areas in the Harvard Forest footprint. The complete set of flux cycles used as input for the model is shown in Figure 5.7.

Along with the magnitude of flux from the landscape and the type of landscape, the height of the PBL determines the change in CO₂ and O₂ mixing ratios that results from a given flux. This height, which determines the volume into which surface O₂ and CO₂ fluxes are mixed, varies at several time scales, including a daily cycle, variation between days due to cloud cover, fronts, and storms, and seasonal variation with changes in day length [e.g. Stull, 2006]. We determined a representative daily profile for the PBL height using meteorological data (NAM 12 km) downloaded from the NOAA Air Resources Laboratory (ARL) archives. The data set has a temporal resolution of 3 hours and a spatial resolution of 12 km. We looked at PBL height for a subsample of dates, including 36 days in winter and 36 days in summer, and calculated an hourly climatology separately for each season (Figure 5.8).

We ran the model for 24 hours after spin-up time, plotted the concentrations of O₂ and CO₂, and calculated the stoichiometric ratio for the same daytime and nighttime intervals as for the observed data. To determine the sensitivity of the model to input
Figure 5.7: $\text{CO}_2$ and $\text{O}_2$ flux cycles used as input for the box model. Solid lines show $\text{CO}_2$ fluxes and dot-dash lines show corresponding $\text{O}_2$ fluxes calculated using the appropriate stoichiometric ratio. The top panel shows forest fluxes, separated into winter and summer cycles, and the bottom panel shows fossil fuel fluxes for an urban and suburban area. Although urban and suburban cycles do vary seasonally, the change is not as pronounced as the biospheric variability and is not essential for our simple model.
Figure 5.8: Daily cycles in PBL height for summer and winter calculated from ARL data [NOAA, 2017]. The black dots show hourly values (with a resolution of three hours) for 36 days during each season, and the blue line shows the average for each hour (with points every three hours connected by a linear interpolation). The summer PBL height is more variable, with lows in the morning and highs in the afternoon driven by radiative heating of the land, whereas the winter profile is relatively flat.
parameters, we varied the landscape composition, flux magnitude, and PBL height. As discussed above, the characteristics of the source region for air “entering” the model also impact the range of variability produced, but we used a constant source region to focus on the variability produced by local exchange alone in the 6-hour intervals.

5.4 Discussion of model results

There are three factors in our model that can cause slopes to differ from the input stoichiometric ratios: variability in landscape composition (changing fractions of urban and forest), variability in the fluxes for a given landscape type (e.g. winter forest vs. summer forest), and variability in the height of the PBL. Importantly, in addition to determining the measured slopes, these factors also determine the range of $\text{O}_2$ and $\text{CO}_2$ mixing ratios that the model produces.

For any PBL height and flux magnitude, a landscape of pure forest produces the expected slope value of -1.05 (Figure 5.9). A purely urban landscape produces the expected slope of -1.4 (Figure 5.10). We would expect mixed landscapes to produce intermediate slopes; however, in addition to the stoichiometry of the landscape fluxes, the slope depends on the relative magnitudes of the fluxes from urban and forested landscapes. Thus, a half-urban, half-forested landscape does not necessarily produce a slope halfway between -1.4 and -1.05. During the summer, when forest and urban fluxes are comparable, the slope is indeed intermediate (-1.33 at night, -1.18 during the day; Figure 5.11). However, during the winter when forest fluxes are consistently low, a small amount of urban influence can have a large effect on the slope value. Five boxes of urban landscape out of thirty, analogous to the passage of air parcels over a small city such as Albany or Springfield, produce a slope of -1.5, showing a strong fossil fuel influence (Figure 5.12).
In some cases, including the last scenario described above, the slope is actually outside the range of the two input stoichiometries. This results from the combined effects of the daily cycles in fluxes and the use of a constant source term for the model. For the winter scenario depicted in Figure 5.12, a parcel of air moving through the early-morning landscape arrives at Harvard Forest considerably enriched in CO₂ and depleted in O₂, relative to the “source region” concentration, because of the peak in urban CO₂ fluxes in the morning. During these early-morning hours, points on the plot evolve down-to-the-right with a slope near -1.4. As the morning progresses, parcels pass over the landscape at a time of smaller urban fluxes and larger forest fluxes. Points on the plot thus evolve up-to-the-left with a slope near -1.05. Taken over the entire interval, with no chronological information, the points have curvature (or simply scatter) and a straight-line fit yields a slope outside the expected range. This is one particular scenario that leads to seemingly implausible slopes, but similar arguments apply in different seasons and at different times of day. In short, real processes can lead to slopes steeper than fossil fuel combustion or shallower than forest exchange. They do not point to problems with the box model.

As discussed in the introduction to this chapter, our primary objective for the model is to characterize the range of CO₂ and O₂ variability due to local sources. With this in mind, we note that changes in the magnitude of the forest and urban fluxes as well as the PBL height also influence the range of CO₂ and O₂ variability. For example, summer PBL values tend to generate larger ranges in CO₂ and O₂ than winter values, because the top of the PBL dips to lower heights at night and in the early morning, amplifying the effects of surface fluxes at those times. This nighttime amplification turns out to be more important than the flux dilution that occurs on summer afternoons due to a relatively high PBL. Because of PBL dynamics, as well as daily cycles in surface fluxes, CO₂ and O₂ ranges during the daytime interval tend to be larger than those during the nighttime interval.
Figure 5.9: Model output for a forested landscape, showing the resulting scatterplots of O$_2$ vs. CO$_2$ for the same daytime and nighttime intervals used with the observed data. The color of the points indicates the time each arrived at Harvard Forest, with the labels on the colorbar denoting hours of the day. Note the decrease followed by an increase in CO$_2$ during the daytime interval and the consistent increase in CO$_2$ during the nighttime interval. The red line shows the linear regression associated with the slope value. This plot was produced using the summer PBL height and summer forest flux cycle. A completely forested landscape produces the expected slope of -1.05, reflecting the stoichiometric ratio of the forest fluxes used to drive the model.
Figure 5.10: Model output for an urban landscape, using the winter PBL height and urban flux cycle. A completely urban landscape produces the expected slope of -1.4.
Figure 5.11: Model output for a mixed landscape consisting of 15 boxes of urban landscape followed by 15 boxes of summer forest, using the summer PBL height cycle. Because the summer forest fluxes are of similar magnitude to the urban fluxes, the slope produced is intermediate between -1.05 and -1.4, the input stoichiometries of the two landscape types.
Figure 5.12: Model output for a mixed landscape consisting of 5 boxes of urban landscape followed by 25 boxes of winter forest, using the winter PBL height cycle. The resulting slopes are outside the range of the two input stoichiometries (-1.05 to -1.4), because the use of a constant source term for the model results in alternating increases and decreases in CO$_2$ and O$_2$ throughout the day based on the daily flux cycles, producing point patterns outside of a straight line and slope values outside the range of the inputs.
The model output is quite sensitive to the PBL height; a 50% reduction in PBL height causes a 100% increase in CO$_2$ and O$_2$ ranges, while a 150% increase in PBL causes a 30% reduction in the ranges. The magnitude of fluxes has a similar impact on observed CO$_2$ and O$_2$ ranges, with increased fluxes leading to larger ranges and vice versa. The phasing of PBL height relative to the flux cycles is also important. A 5-hour shift in the PBL cycle produces unphysical plots with concurrent increases in CO$_2$ and O$_2$ because of the unnatural offset between the flux cycles and the PBL cycles.

By comparing the range of CO$_2$ and O$_2$ predicted by the model with the ranges we observe in our slope data, we can determine whether the observed range of variability can be attributed to local influence alone or whether an additional contribution from background variability is required. Results of multiple model runs and sensitivity tests are summarized in Table 5.1. For summer conditions, the model produces CO$_2$ variability of about 4–16 ppm and O$_2$ variability of about 5–20 ppm (although the range for both is sometimes as low as 2 ppm at night). Winter ranges are smaller, on the order of 1–5 ppm for CO$_2$ and 1–6 ppm for O$_2$. If observed ranges of CO$_2$ and O$_2$ are similar to those produced by the model, this supports the conclusion that local influence drives the observed changes in mixing ratios; if the observed ranges are larger, this suggests an additional contribution from background variability.

For comparison with observed data, we recorded and analyzed the range of CO$_2$ and O$_2$ for each of the 3760 slope plots. For each plot, we calculated the range between the 95th and 5th percentiles for the CO$_2$ and O$_2$ values in each 6-hour interval. By using percentiles, we hoped to reduce the impact of outlier data points on the resulting ranges. However, because of some plots with anomalously high CO$_2$ and O$_2$ data points, the distribution of ranges includes some large values and is strongly right-skewed (Figure 5.13). We therefore used the median as a measure of central tendency. The median CO$_2$ range is about 8 ppm, and the median O$_2$ range is about 14 ppm.
Table 5.1: Summary of CO₂ and O₂ ranges and slopes for daytime and nighttime intervals produced by the model for a range of landscape compositions, PBL heights, and flux magnitudes. Summer ranges tend to be larger than winter ranges, and daytime ranges tend to be slightly larger than nighttime ranges. Increases in the magnitude of the fluxes or decreases in the PBL height result in increased ranges.
Figure 5.13: Histograms showing the distribution of CO\textsubscript{2} and O\textsubscript{2} ranges for the full set of 6-hour slope values. Top two panels show normal probability plots, where the dashed line describes a normal distribution. CO\textsubscript{2} ranges are slightly lower than O\textsubscript{2} ranges overall. One outlier in the normal probability plots with a CO\textsubscript{2} range of 15080 ppm and an O\textsubscript{2} range of 24760 µmol/mol was omitted for clarity, and the upper tail of the histograms was omitted to better show the distribution of the core of the data.
The observed CO\textsubscript{2} and O\textsubscript{2} variability is consistent with the variability produced by the model under a range of conditions. Although many of the CO\textsubscript{2} and O\textsubscript{2} ranges for individual 6-hour intervals are larger than those produced by the model, the distribution supports the conclusion that a substantial portion of our slopes reflect a strong local signal.

If the model more realistically included small changes in the concentration of “source region” air, this would only increase the modeled ranges, further supporting the notion that we do observe 6-hour intervals dominated by local influence at our site. Alternatively, if we were to limit our observations to periods with “stable” meteorology, we might well reduce the high side of the range and improve data-model agreement. The latter possibility is discussed further below.
Chapter 6

Isolating periods of local influence to better measure $\alpha_b$

6.1 Introduction

Based on the model results, local exchange produces CO$_2$ and O$_2$ variability that is similar to the median ranges in our observed data. However, many of the slope values from the observed data have ranges larger than the values that characterize local influence, and these plots must therefore be driven by background variability as well as local exchange. In particular, many of our winter plots have CO$_2$ and O$_2$ ranges much larger than those predicted by local exchange alone. In order to more accurately determine the value of $\alpha_b$, we attempt to remove those slopes influenced by changes in the source region and focus on slopes dominated by local exchange. For this analysis, we use the iteratively cut data set from which the averages described in Section 3.3 were derived.

6.2 Slopes categorized by friction velocity

To filter slopes dominated by background variability out of the dataset, we first used threshold values for $u^*$. Friction velocity reflects turbulent motion in the air, so that large
values of $u^*$ are associated with more mixed conditions and low values are associated with more stratified conditions. We hypothesized that periods with low $u^*$ would be more likely to reflect local influences, and thus contain slope values that are closer to $\alpha_b$. We used the same $u^*$ data from the Harvard Forest EMS tower referenced earlier [see Section 3.1; Munger, 2018] to match individual $u^*$ values to individual gas concentration data points. Each CO$_2$/O$_2$ data point was matched to a $u^*$ value using the hour of the time at which the CO$_2$/O$_2$ data point was collected. Then the average, maximum, and standard deviation in $u^*$ were calculated for each 6-hour interval, associating values for this set of parameters with each slope value. Maximum $u^*$ may reveal the occurrence of gusts that disturb canopy stratification, while $\sigma_{u^*}$ may similarly reflect instability that would not be evident from a simple average. Because $u^*$ tends to be higher during the winter, this filter may also emphasize summer slopes whose CO$_2$ and O$_2$ ranges reflect more of a local influence.

Efforts to categorize slopes based on $u^*$ were inconclusive. There was little difference between slopes split using thresholds of 40 cm/s for average $u^*$, 50 cm/s for maximum $u^*$, and 10 cm/s for $\sigma_{u^*}$. Although we expected higher values of these parameters to be associated with steeper slopes, due to windy conditions increasing turbulent exchange with air outside the canopy layer and increasing the footprint for a given time period, in some cases the slopes with lower $u^*$ values had a slightly more negative mean. The high variability in $u^*$ within each daily period and its sensitivity to wind gusts may in fact weaken this parameter’s ability to distinguish between local and background influence by being overly sensitive, or $u^*$ may simply not be closely related to the size of the tower’s footprint for a given 6-hour period. A scatter plot of CO$_2$ ranges against average $u^*$ showed no significant positive relationship, indicating that $u^*$ may not provide a useful filter for selecting periods of local influence. Because the sensor for $u^*$ is located above the canopy, it may not reflect air movement dynamics at the low intake, which may further obscure any relationship between $u^*$ and slopes.
6.3 Slopes filtered by CO$_2$ range

Because CO$_2$ and O$_2$ ranges are also a metric of the amount of local influence vs. background variability, we filtered slopes by CO$_2$ range. We performed this process separately by season, because the CO$_2$ and O$_2$ ranges expected for local influence are much smaller during the winter. Results of this range-based filtering are shown in Table 6.1.

For the summer, slopes with low CO$_2$ ranges have a less negative mean than those with higher CO$_2$ ranges, using a threshold of 10 ppm. Although there are fewer slopes for the low range subset than the high range (176 vs. 831), the dataset for the low CO$_2$ range is still large enough to maintain statistical significance.

For the winter dataset, fewer slopes are available, but the slopes with lower CO$_2$ ranges still have a less negative average value than the slopes with higher CO$_2$ ranges, using a threshold of 4 ppm. The difference between the two averages is enhanced compared to the summer, despite a steeper average slope for the low-range subset compared to the summer low-range subset. We speculate that this steeper slope for the winter low-range subset is due to the higher likelihood of fossil fuel signal contaminating the observed O$_2$ : CO$_2$ exchange ratio. A potential increase in the influence of soil respiration in winter may also result in a different average exchange ratio than in the summer.

<table>
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<th>Filter</th>
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<th>median</th>
<th>SD</th>
<th>SEM</th>
<th>N</th>
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<td>-1.00</td>
<td>0.30</td>
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<td>CO$_2$ range &gt; 10 ppm</td>
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<td>-1.06</td>
<td>0.19</td>
<td>0.01</td>
<td>831</td>
</tr>
<tr>
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<td>-1.10</td>
<td>0.48</td>
<td>0.04</td>
<td>188</td>
</tr>
<tr>
<td></td>
<td>CO$_2$ range &gt; 4 ppm</td>
<td>-1.16</td>
<td>-1.18</td>
<td>0.39</td>
<td>0.02</td>
<td>253</td>
</tr>
</tbody>
</table>

Table 6.1: Slopes filtered by CO$_2$ range and season. For the summer, a range of 10 ppm or less in CO$_2$ should reflect local influence, based on our model results, whereas for winter, the threshold is lower, about 4 ppm. As expected, the average slope values for the low CO$_2$ range subsets were shallower than those for the high CO$_2$ range subsets. The summer slope values were also shallower than the winter values, perhaps an indication of fossil fuel influence during the winter. SD is standard deviation, SEM is standard error of the mean.
Chapter 7

Conclusion

Our results indicate that the use of atmospheric data to estimate the value of $\alpha_b$ is a promising technique that may complement elemental analysis techniques. Based on our average value for the exchange ratio, we suggest that the true value of $\alpha_b$ may be lower than the accepted value of 1.1, at least for a temperate deciduous forest ecosystem, with a potential range of 1.00 to 1.06. Some evidence of seasonal cycles as well as significantly different average slope values for winter and summer suggest that the value of the $O_2 : CO_2$ exchange ratio varies seasonally. Possible drivers include variation in biospheric processes, such as changes in the types of molecules produced by plants and the influence of soil respiration, as well as an increase in fossil fuel influence during the winter due to the reduced magnitude of biospheric fluxes. Based on the results of a simple one-dimensional box model, we estimated the range of $CO_2$ and $O_2$ variability that could plausibly result from local exchange alone, and we used this range to obtain a subset of slopes with $CO_2$ ranges indicative of a strong local signal. The average value of these slopes for the summer months, 1.00 ± 0.02, constitutes our best estimate for the value of $\alpha_b$ for a summer biosphere, the time when biospheric processes are most active. We speculate that our winter value of 1.06 may be contaminated by a fossil fuel signal and may not reflect a purely biospheric respiration signal.
The atmospheric measurement technique, although complex in interpretation, offers valuable insight for a seasonal- and ecosystem-averaged value of $\alpha_b$. This average value is particularly useful for carbon sink calculations, which lump the entire terrestrial biosphere carbon uptake as a single term. In a previous study, Seibt et al. [2004] discounted the use of canopy air measurements to determine the $O_2 : CO_2$ exchange ratio for the terrestrial biosphere, due to canopy air consisting of mixed exchange ratios from plants, soil, and air introduced from outside the canopy by turbulent exchange. However, this earlier work did not include long time series measurements. Although background variation may influence some of our observed slopes, careful consideration of atmospheric conditions and CO$_2$ ranges allows for the selection of periods dominated by a local signal. In fact, the spatiotemporally-averaged nature of our value of $\alpha_b$ is one of its strengths. By encompassing all types of carbon assimilation and respiration for a particular ecosystem over time, our method avoids the need to quantify separate contributions from various carbon pools (trees, soil, understory plants, etc.) and from various processes within each pool (production of glucose, lignin, etc.) to the overall exchange ratio.

Further investigation into data filtering methods that isolate periods of local influence may enhance the applicability of concurrently-measured atmospheric O$_2$ and CO$_2$ data as a measurement of $\alpha_b$. One technique may be to use slopes from stagnant summer periods with high pressure, when wind speeds are low, CO$_2$ and O$_2$ ranges are small, and local influence is likely dominant. Another potential technique could use the high intake, which tends to have higher CO$_2$ and O$_2$ variability, as a reference or background measurement, and look at the difference between the low intake and the high intake as an indicator of local influence at the low intake. Selecting a study site that is more isolated from fossil fuel activity may also provide a more accurate measurement of $\alpha_b$, although such sites are not available for all ecosystem types. Use of concurrent measurements of CO as a tracer of fossil fuel signal could help filter out time intervals significantly influenced by fossil fuels [Potosnak et al., 1999].
Recent research suggests that species type rather than climate has a strong influence on the O$_2$ : CO$_2$ exchange ratio in different ecosystems [Gallagher et al., 2017]. Atmospheric measurements in a range of ecosystem types, from tropical forests to tundra, would therefore provide important information on global variability in $\alpha_b$, allowing for the calculation of a composite value for $\alpha_b$ [as in Worrall et al., 2013] that takes into account the known distributions of different ecosystem types. A more accurate value for $\alpha_b$ will improve our knowledge of the land carbon sink and forecasts for future atmospheric CO$_2$ levels. In our rapidly changing climate and world, this knowledge is critical for both mitigation and adaptation efforts.
Appendix A

Black & White Figures

Figure A.1: Map showing the location of the Harvard Forest EMS tower and Bowdoin College (Figure 2.1).
Figure A.2: Photograph of the aspirated inlet at the high intake, designed to reduce thermal fractionation. Image credit: Mark Battle (Figure 2.2).

Figure A.3: Plot of CO$_2$ vs. time for a calibration run, showing the curve fitted to the data points about which the scatter is calculated to determine the instrumental error in CO$_2$ measurements (Figure 2.4).
Figure A.4: Error in CO$_2$ (top) and O$_2$ (bottom) plotted against serial number, which corresponds to the chronological order of data points. Error varied over time and tended to increase significantly at the end of the study period. We speculate that this increase in error may be due to problems with system gas tightness (Figure 2.5).
Figure A.5: Example of scatterplots of O\textsubscript{2} vs. CO\textsubscript{2} for the four subsets of data: day and night at high and low intakes. These plots are for 9am–3pm on 21 July and 10pm–4am on 21–22 July in 2007. The shading of the points indicates the time at which each data point was taken (in local time). Note the overall decrease in CO\textsubscript{2} and increase in O\textsubscript{2} during the daytime interval, driven by photosynthesis, and the overall increase in CO\textsubscript{2} and decrease in O\textsubscript{2} during the nighttime interval, driven by respiration. The line shows the results of a Deming regression (described in Section 3.1), and the slope, corresponding to the O\textsubscript{2} : CO\textsubscript{2} exchange ratio, is indicated above each plot (Figure 3.1).
Figure A.6: Hourly values of friction velocity ($u^*$, cm/s). Points show hourly $u^*$ values for 1991-2015 measured at the Harvard Forest EMS tower, and the line shows the hourly average. Although $u^*$ is highly variable, with a large amount of scatter for each hour of the day, standard errors on the hourly averages are too small to be seen on the plot, and the climatology is well constrained (Figure 3.2).
Figure A.7: Seasonal variability in $u^*$ (cm/s). Points show the average $u^*$ value for each day of the year, calculated from hourly data for 1991-2015. The line shows the results of a loess smoothing function using a window of 36.5 days. Friction velocity tends to be higher and more variable in the winter months compared to the summer (Figure 3.3).

Figure A.8: Scatterplots of $O_2$ vs. $CO_2$ for 14–15 June 2012 at the low intake. The empty circle denotes a point that was removed by the orthogonal residual cut and was not included in the final fit shown by the line (Figure 3.4).
Figure A.9: Distribution of slopes for the entire dataset after the iterative cut. The top left panel shows the iteratively cut slopes plotted against time in decimal years; gaps indicate periods where no data were collected. The top right panel shows a histogram of the iteratively cut slopes. The bottom left panel shows a normal probability plot for the entire dataset after the first iteration of the iterative cut, whereas the bottom right shows the same plot after the iterative cut was completed, demonstrating the reduction of the dataset’s non-Gaussian tails. The dotted lines in the normal probability plots indicate the point pattern expected for a normal distribution. Summary statistics are in Table 3.1 (Figure 3.5).
Figure A.10: Histograms and normal probability plots for the four data subsets. Each normal probability plot corresponds to the histogram to its left. Although the iterative cut partially normalizes the distributions, there are still non-Gaussian tails, visible in the normal probability plots, in which the dotted line indicates the point pattern expected for a normal distribution. For this reason, we include both the means and the medians for comparison in the summary statistics in Table 3.1 (Figure 3.6).
Figure A.11: Plot of slopes vs. time in decimal date. Point shading indicates the time interval and intake height for each data point. The increase in spread towards the end of the study period may be a reflection of the increase in measurement error shown in Figure 2.5 (Figure 3.7).

Figure A.12: Scatterplot of $O_2$ vs. $CO_2$ for the nighttime interval on 15–16 October 2008. Although the linear fit is obviously inappropriate for this plot, the uncertainty in the regression is low. This is due to the anomalously large ranges in $CO_2$ and $O_2$, which are much higher than the ranges characteristic of the majority of the plots (Figure 3.8).
Figure A.13: Scatterplots of O₂ vs. CO₂ for 3–4 October 2007. In the “Day, High Intake” plot, an anomalously high CO₂ value resulted in a non-representative fit without much increasing the uncertainty, while the other subsets, whose linear fits are much more representative of the trend in the data, have higher uncertainties. Similar to Figure 3.8, a point with a much higher CO₂ or O₂ value than the rest of the data causes problems for the linear regression and results in low uncertainties that do not reflect the actual quality of the fit (Figure 3.9).
Figure A.14: Histograms for winter and summer slope values. Winter comprises the months of December, January, and February and summer comprises June, July, and August. Winter slopes have a more negative mean value, closer to the stoichiometric ratio for fossil fuel combustion, although the sample size is smaller for winter than for summer. Statistics are shown in Table 4.1 (Figure 4.4).
Figure A.15: 24-hour back-trajectories for Harvard Forest produced by the HYSPLIT model, starting on 18 December 2012. Each trajectory shows the path of an air parcel during the 24 hours before it arrived at Harvard Forest. Trajectories were started at 6-hour intervals, moving back in time, to create the ensemble of trajectories shown. For this longer time period, the source region is highly variable and encompasses a large area, demonstrating our rationale for using a shorter 6-hour interval for our slope plots to reduce source region variability (Figure 5.1).
Figure A.16: A set of 48 6-hour back-trajectories produced by the Hysplit model, plotted on satellite imagery from Google Earth. Each trajectory shows the path of an air parcel during the 6-hour period before it arrives at Harvard Forest. Trajectories include 24 daytime and 24 nighttime trajectories for two days in winter and two days in summer. For each day, trajectories were started each hour between 9am–3pm and 10pm–4am, the same time intervals used for the slope plots. These 6-hour intervals encompass a fairly consistent source region with a radius of 50–200 km. The area is mostly forested with some small urban centers (Figure 5.2).
Figure A.17: 6-hour back trajectories for Harvard Forest on 24 Jan 2009, with one trajectory started each hour between 9am and 3pm EST (corresponding to the 6-hour daytime interval used to calculate slopes), showing variability in the source region over that time period. This particular day shows a steady shift in the source region over time, although the path length and general source area remain similar. For this period, background variability might have a slightly stronger influence on the observed CO\textsubscript{2} and O\textsubscript{2} variability at Harvard Forest (Figure 5.3).
Figure A.18: 6-hour back trajectories for Harvard Forest on 2 Feb 2015, with one trajectory started each hour between 10pm and 4am EST (corresponding to the 6-hour nighttime interval used to calculate slopes), showing variability in the source region over that time period. For this particular night, changes in the source region were minimal, with air coming from a small area in southwestern NH, so local influence would likely dominate the observed CO$_2$ and O$_2$ variability at Harvard Forest (Figure 5.4).
Figure A.19: A conceptual diagram of the box model. Only 6 of the 30 boxes are shown, denoting the locations of the air parcel at each hour along its path to Harvard Forest. Air enters the model from the left (the source region) and leaves the model on the right (at Harvard Forest). As the air parcels travel through each box, O$_2$ and CO$_2$ are exchanged between the boxes and the landscape, which changes the mixing ratio of the parcel. The parcels shift forward every 12 minutes, and their mixing ratios are recorded as they arrive in the final “Harvard Forest” box on the right (Figure 5.5).
Figure A.20: An hourly climatology of CO$_2$ fluxes at Harvard Forest based on hourly eddy flux data from 1991–2015, separated into winter and summer climatologies. Points show the ensemble of hourly data points, and the line shows the average value for each hour. Summer fluxes have much higher magnitudes and a more pronounced daily cycle than winter fluxes, which are low, slightly positive (due to respiration) and fairly constant. One outlier in the summer plot (hour 23, flux 107.7 µmol CO$_2$/m$^2$/s) was omitted for clarity (Figure 5.6).
Figure A.21: CO$_2$ and O$_2$ flux cycles used as input for the box model. Lines show CO$_2$ fluxes and corresponding O$_2$ fluxes calculated using the appropriate stoichiometric ratio. The top panel shows forest fluxes, separated into winter and summer cycles, and the bottom panel shows fossil fuel fluxes for an urban and suburban area. Although urban and suburban cycles do vary seasonally, the change is not as pronounced as the biospheric variability and is not essential for our simple model (Figure 5.7).
Figure A.22: Daily cycles in PBL height for summer and winter calculated from ARL data [NOAA, 2017]. The points show hourly values (with a resolution of three hours) for 36 days during each season, and the line shows the average for each hour (with points every three hours connected by a linear interpolation). The summer PBL height is more variable, with lows in the morning and highs in the afternoon driven by radiative heating of the land, whereas the winter profile is relatively flat (Figure 5.8).
Figure A.23: Model output for a forested landscape, showing the resulting scatterplots of O\(_2\) vs. CO\(_2\) for the same daytime and nighttime periods used with the observed data. The shading of the points indicates the time each arrived at Harvard Forest, with the labels on the colorbar denoting hours of the day. The line shows the linear regression associated with the slope value. This plot was produced using the summer PBL height and summer forest flux cycle. A completely forested landscape produces the expected slope of -1.05, reflecting the stoichiometric ratio of the forest fluxes used to drive the model (Figure 5.9).
Figure A.24: Model output for an urban landscape, using the winter PBL height and urban flux cycle. A completely urban landscape produces the expected slope of -1.4 (Figure 5.10).
Figure A.25: Model output for a mixed landscape consisting of 15 boxes of urban landscape followed by 15 boxes of summer forest, using the summer PBL height cycle. Because the summer forest fluxes are of similar magnitude to the urban fluxes, the slope produced is intermediate between -1.05 and -1.4, the input stoichiometries of the two landscape types (Figure 5.11).
Figure A.26: Model output for a mixed landscape consisting of 5 boxes of urban landscape followed by 25 boxes of winter forest, using the winter PBL height cycle. The resulting slopes are outside the range of the two input stoichiometries (-1.05 to -1.4), because the use of a constant source term for the model results in alternating increases and decreases in \( \text{CO}_2 \) and \( \text{O}_2 \) throughout the day based on the daily flux cycles, producing point patterns outside of a straight line and slope values outside the range of the inputs (Figure 5.12).
Figure A.27: Histograms showing the distribution of CO₂ and O₂ ranges for the full set of 6-hour slope values. Top two panels show normal probability plots, where the dashed line describes a normal distribution. CO₂ ranges are slightly lower than O₂ ranges overall. One outlier in the normal probability plots with a CO₂ range of 15080 ppm and an O₂ range of 24760 µmol/mol was omitted for clarity, and the upper tail of the histograms was omitted to better show the distribution of the core of the data (Figure 5.13).
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